

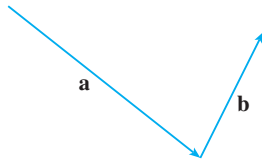
EXERCISES

- (a) Find an equation of the sphere that passes through the point $(6, -2, 3)$ and has center $(-1, 2, 1)$.
 (b) Find the curve in which this sphere intersects the yz -plane.
 (c) Find the center and radius of the sphere

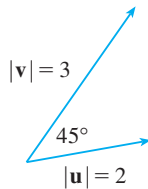
$$x^2 + y^2 + z^2 - 8x + 2y + 6z + 1 = 0$$

- Copy the vectors in the figure and use them to draw each of the following vectors.

- (a) $\mathbf{a} + \mathbf{b}$ (b) $\mathbf{a} - \mathbf{b}$ (c) $-\frac{1}{2}\mathbf{a}$ (d) $2\mathbf{a} + \mathbf{b}$



- If \mathbf{u} and \mathbf{v} are the vectors shown in the figure, find $\mathbf{u} \cdot \mathbf{v}$ and $|\mathbf{u} \times \mathbf{v}|$. Is $\mathbf{u} \times \mathbf{v}$ directed into the page or out of it?



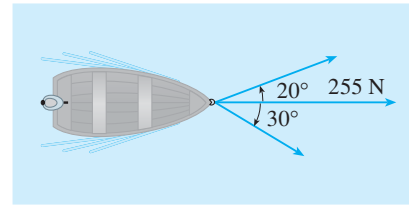
- Calculate the given quantity if

$$\mathbf{a} = \mathbf{i} + \mathbf{j} - 2\mathbf{k} \quad \mathbf{b} = 3\mathbf{i} - 2\mathbf{j} + \mathbf{k} \quad \mathbf{c} = \mathbf{j} - 5\mathbf{k}$$

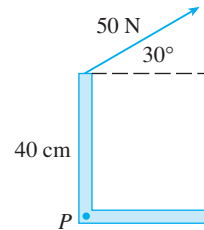
- $2\mathbf{a} + 3\mathbf{b}$
 - $|\mathbf{b}|$
 - $\mathbf{a} \cdot \mathbf{b}$
 - $\mathbf{a} \times \mathbf{b}$
 - $|\mathbf{b} \times \mathbf{c}|$
 - $\mathbf{a} \cdot (\mathbf{b} \times \mathbf{c})$
 - $\mathbf{c} \times \mathbf{c}$
 - $\mathbf{a} \times (\mathbf{b} \times \mathbf{c})$
 - $\text{comp}_{\mathbf{a}} \mathbf{b}$
 - $\text{proj}_{\mathbf{a}} \mathbf{b}$
 - The angle between \mathbf{a} and \mathbf{b} (correct to the nearest degree)
- Find the values of x such that the vectors $\langle 3, 2, x \rangle$ and $\langle 2x, 4, x \rangle$ are orthogonal.
 - Find two unit vectors that are orthogonal to both $\mathbf{j} + 2\mathbf{k}$ and $\mathbf{i} - 2\mathbf{j} + 3\mathbf{k}$.
 - Suppose that $\mathbf{u} \cdot (\mathbf{v} \times \mathbf{w}) = 2$. Find
 - $(\mathbf{u} \times \mathbf{v}) \cdot \mathbf{w}$
 - $\mathbf{u} \cdot (\mathbf{w} \times \mathbf{v})$
 - $\mathbf{v} \cdot (\mathbf{u} \times \mathbf{w})$
 - $(\mathbf{u} \times \mathbf{v}) \cdot \mathbf{v}$
 - Show that if \mathbf{a} , \mathbf{b} , and \mathbf{c} are in V_3 , then

$$(\mathbf{a} \times \mathbf{b}) \cdot [(\mathbf{b} \times \mathbf{c}) \times (\mathbf{c} \times \mathbf{a})] = [\mathbf{a} \cdot (\mathbf{b} \times \mathbf{c})]^2$$
 - Find the acute angle between two diagonals of a cube.
 - Given the points $A(1, 0, 1)$, $B(2, 3, 0)$, $C(-1, 1, 4)$, and $D(0, 3, 2)$, find the volume of the parallelepiped with adjacent edges AB , AC , and AD .

- (a) Find a vector perpendicular to the plane through the points $A(1, 0, 0)$, $B(2, 0, -1)$, and $C(1, 4, 3)$.
 (b) Find the area of triangle ABC .
- A constant force $\mathbf{F} = 3\mathbf{i} + 5\mathbf{j} + 10\mathbf{k}$ moves an object along the line segment from $(1, 0, 2)$ to $(5, 3, 8)$. Find the work done if the distance is measured in meters and the force in newtons.
- A boat is pulled onto shore using two ropes, as shown in the diagram. If a force of 255 N is needed, find the magnitude of the force in each rope.



- Find the magnitude of the torque about P if a 50-N force is applied as shown.



- 15–17 ■ Find parametric equations for the line.

- The line through $(4, -1, 2)$ and $(1, 1, 5)$
- The line through $(1, 0, -1)$ and parallel to the line $\frac{1}{3}(x - 4) = \frac{1}{2}y = z + 2$
- The line through $(-2, 2, 4)$ and perpendicular to the plane $2x - y + 5z = 12$

- 18–20 ■ Find an equation of the plane.

- The plane through $(2, 1, 0)$ and parallel to $x + 4y - 3z = 1$
 - The plane through $(3, -1, 1)$, $(4, 0, 2)$, and $(6, 3, 1)$
 - The plane through $(1, 2, -2)$ that contains the line $x = 2t$, $y = 3 - t$, $z = 1 + 3t$
21. Find the point in which the line with parametric equations $x = 2 - t$, $y = 1 + 3t$, $z = 4t$ intersects the plane $2x - y + z = 2$.
22. Find the distance from the origin to the line $x = 1 + t$, $y = 2 - t$, $z = -1 + 2t$.