

Homework 12 Supplementary Problems

1. Prove that $|[0, 1)| = |[0, 1]|$.
2. A number $r \in \mathbb{R}$ is called *algebraic* if $\exists n \in \mathbb{N}, a_0, \dots, a_n \in \mathbb{Z}$, such that

$$a_0 r^n + a_1 r^{n-1} + \dots + a_n = 0.$$

Prove that the set of algebraic numbers is denumerable.